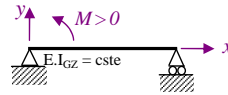


Formulaire des flèches et rotations de poutres isostatiques :

Poutres :

- portée L ;
- module d'Young du matériau : E ;
- moment quadratique de la section : I_{GZ} ;

- repère :



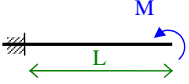
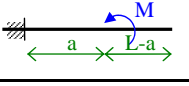

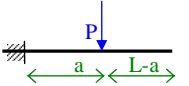
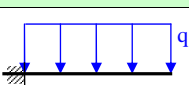
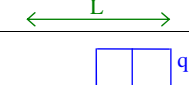
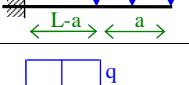
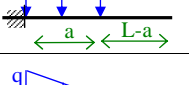
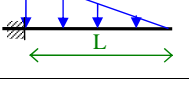
1) Poutres sur 2 appuis

| Schémas | Flèches (f) | Rotations (ω) |
|--------------------------------|---|--|
| Chargements : moments : | | |
| | $f_{\max} = f_{(L/\sqrt{3})} = -\frac{M \times L^2}{9\sqrt{3} \times E \times I_{GZ}}$ $f_{(L/2)} = -\frac{M \times L^2}{16 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{M \times L}{3 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{M \times L}{6 \times E \times I_{GZ}}$ |
| | $f_{(L/2)} = 0$ | $\omega' = \omega_{(0)} = \frac{M \times L}{24 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{M \times L}{24 \times E \times I_{GZ}}$ |
| | $f_{(L/2)} = -\frac{(M_A + M_B) \times L^2}{16 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{(2 \times M_A + M_B) \times L}{6 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{(M_A + 2 \times M_B) \times L}{6 \times E \times I_{GZ}}$ |

| | | |
|--|--|--|
| Chargements : charges linéiques : | | |
| | $f_{\max} = f_{(L/2)} = -\frac{5 \times q \times L^4}{384 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{q \times L^3}{24 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{q \times L^3}{24 \times E \times I_{GZ}}$ |
| | $f_{\max} = f_{(L/2)} = -\frac{q \times L^4}{120 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{5 \times q \times L^3}{192 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{5 \times q \times L^3}{192 \times E \times I_{GZ}}$ |
| | $f_{\max} = f_{(L/2)} = -\frac{3 \times q \times L^4}{640 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{q \times L^3}{64 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{q \times L^3}{64 \times E \times I_{GZ}}$ |
| | $f_{\max} = f_{(0,5193L)} = -\frac{q \times L^4}{153,3 \times E \times I_{GZ}}$ $f_{(L/2)} = -\frac{5 \times q \times L^4}{768 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{7 \times q \times L^3}{360 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{q \times L^3}{45 \times E \times I_{GZ}}$ |

| Schémas | Flèches (f) | Rotations (ω) |
|---|---|--|
| Chargements : forces ponctuelles : | | |
| | $f_{\max} = f_{(L/2)} = -\frac{P \times L^3}{48 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{P \times L^2}{16 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{P \times L^2}{16 \times E \times I_{GZ}}$ |
| | $f_{\max} = f_{(\frac{L^2-b^2}{3})} = -\frac{P \times b \times (L^2 - b^2)^{3/2}}{9\sqrt{3} \times L \times E \times I_{GZ}}$ $f_{(a)} = -\frac{P \times a^2 \times b^2}{3 \times L \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{P \times a \times b \times (L + b)}{6 \times L \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{P \times a \times b \times (L + a)}{6 \times L \times E \times I_{GZ}}$ |
| | $f_{\max} = f_{(L/2)} = -\frac{P \times a \times (3L^2 - 4a^2)}{24 \times E \times I_{GZ}}$ $f_{(a)} = -\frac{P \times a^2 \times (3L - 4a)}{6 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{P \times a \times (L - a)}{2 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{P \times a \times (L - a)}{2 \times E \times I_{GZ}}$ |
| | $f_{\max} = f_{(L/2)} = -\frac{23 \times P \times L^3}{648 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{P \times L^2}{9 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{P \times L^2}{9 \times E \times I_{GZ}}$ |
| | $f_{\max} = f_{(L/2)} = -\frac{19 \times P \times L^3}{384 \times E \times I_{GZ}}$ | $\omega' = \omega_{(0)} = -\frac{5 \times P \times L^2}{32 \times E \times I_{GZ}}$ $\omega'' = \omega_{(L)} = \frac{5 \times P \times L^2}{32 \times E \times I_{GZ}}$ |

II) Consolés

| Schémas | Flèches (f) | Rotations (ω) |
|---|---|---|
| Chargements : moments : | | |
|  | $f_{\max} = f_{(L)} = \frac{M \times L^2}{2 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = \frac{M \times L}{E \times I_{GZ}}$ |
|  | $f_{\max} = f_{(L)} = \frac{M \times a \times (2L - a)}{2 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = \frac{M \times a}{E \times I_{GZ}}$ |
| Chargements : forces ponctuelles : | | |
|  | $f_{\max} = f_{(L)} = -\frac{P \times L^3}{3 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = -\frac{P \times L^2}{2 \times E \times I_{GZ}}$ |
|  | $f_{\max} = f_{(L)} = -\frac{P \times a^2 \times (3 \times L - a)}{6 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = -\frac{P \times a^2}{2 \times E \times I_{GZ}}$ |
| Chargements : charges réparties : | | |
|  | $f_{\max} = f_{(L)} = -\frac{q \times L^4}{8 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = -\frac{q \times L^3}{6 \times E \times I_{GZ}}$ |
|  | $f_{\max} = f_{(L)} = -\frac{q \times a (a^3 - 6a \times L^2 + 8L^3)}{24 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = -\frac{q \times a (a^2 - 3a \times L + 3L^2)}{6 \times E \times I_{GZ}}$ |
|  | $f_{\max} = f_{(L)} = \frac{q \times a^3 (a - 4 \times L)}{24 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = -\frac{q \times a^3}{6 \times E \times I_{GZ}}$ |
|  | $f_{\max} = f_{(L)} = -\frac{q \times L^4}{30 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = -\frac{q \times L^3}{24 \times E \times I_{GZ}}$ |
|  | $f_{\max} = f_{(L)} = -\frac{11 \times q \times L^4}{120 \times E \times I_{GZ}}$ | $\omega'' = \omega_{(L)} = -\frac{q \times L^3}{8 \times E \times I_{GZ}}$ |